DEM-Aided Block Adjustment for Satellite Images With Weak Convergence Geometry

Tee-Ann Teo, Liang-Chien Chen, Chien-Liang Liu, Yi-Chung Tung, and Wan-Yu Wu

Abstract—To acquire the largest possible coverage for environmental monitoring, it is important in most situations that the overlapping areas and the convergent angles of respective satellite images be small. The traditional bundle adjustment method used in aerial photogrammetry may not be the most suitable for direct orientation modeling in situations characterized by weak convergence geometry. We propose and compare three block adjustment methods for the processing of satellite images using the digital elevation model (DEM) as the elevation control. The first of these methods is a revised traditional bundle adjustment approach. The second is based on the direct georeferencing approach. The third is a rational function model with sensor-oriented rational polynomial coefficients. A collocation technique is integrated into all three methods to improve the positioning accuracy. Experimental results indicate that using the DEM as an elevation control can significantly improve the geometric accuracy as well as the geometric discrepancies between images. This is the case for all three methods. Moreover, the geometric performance of the three methods is similar. There is a significant improvement in geometric consistency between overlapping SPOT images with respect to single image adjustment for steep areas.

Index Terms—Digital elevation model (DEM), direct georeferencing, modified bundle adjustment, rational function model (RFM).

I. INTRODUCTION

ONE of the most important applications of satellite images is for landuse/landcover monitoring. It is the case that, due to satellites’ small field of view (FOV), the area of interest often covers two or more images. Thus, mosaicking becomes a must. Another important application of remotely sensed images is detection of change. In this case, multitemporal images should be registered before performing the comparison. Simultaneous block adjustment is the preferred approach to enhancing the quality of this geometric registration. The adjusted orientation parameters provide a sound foundation for rigorous orthorectification. Except for those satellites that are dedicated to digital elevation model (DEM) generation (such as ALOS-PRISM, ASTER, Cartosat-1, SPOT-5 HRS, etc.), it is observed that to acquire the largest possible coverage, the area of overlap of the satellite images should generally be small. In addition, it should be noted that the convergent angles for a stereo model are not always large.

Block adjustment can enhance the geometric consistency between satellite images to increase the accuracy for orientation determination [1]. There are three types of adjustment approaches, namely, bundle adjustment [2]–[4], direct georeferencing [5]–[7], and the rational function model (RFM) [8]. From the photogrammetric point of view, traditional 3-D bundle adjustment is the most mature approach in that the collinearity condition for all of the tie points (TPs) and ground control points (GCPs) are satisfied simultaneously. However, due to the small scene size of the satellites, favorable convergence geometry cannot always be expected. In addition, the area of overlap between satellite strips may not be always large enough. Hence, the bundle adjustment approach needs to be modified to adopt for the weakly convergence geometry.

Orun and Natarajan [9] use collinearity equations and second-order polynomials to describe the dynamic sampling of a linear charge-coupled device (CCD) sensor. The bundle adjustment method is applied to study the SPOT geometry. Their experimental results indicate that a smaller angle of convergence has a significant effect on the elevation accuracy. Their experimental results indicate that a smaller angle of convergence has a significant effect on the elevation accuracy. A weakly convergent angle (i.e., 10°) may cause an elevation error of hundreds of meters.

In direct georeferencing, on the other hand, orbital and attitude data are utilized for orientation modeling. There are increasing amounts of on-board data available due to advances in geographic positioning system (GPS), inertial navigation system (INS), and star tracker technology. Orbital and attitude data provide relatively accurate position and attitude information. Thus, the number of GCPs required for direct georeferencing could be reduced. However, to preserve the accuracy of image parts within the overlapping area of connecting strips, TPs need to be included. Again, some improvements should be added to cope with cases where there is weakly convergence geometry or small overlap.

Due to its simplicity of implementation and standardization, RFM has been widely used in the field of remote sensing. In the RFM, one uses the ratio of two cubic polynomials and the rational polynomial coefficients (RPCs), which are determined by fitting the physical camera model to describe the relationship between object space and image space [10]. To some extent, the RFM may be interpreted as another form of direct...
The major applications for remotely sensed images are for the detection of natural resources and monitoring of the geoenvironment. To acquire the largest possible coverage, the area of overlap of satellite images should be as small as possible. However, weak geometry of the area of intersection will lead to a large elevation error. In other words, the base-to-height ratio of multiorbit satellite images is, frequently, not large enough. Although several investigators have discussed block adjustment methods for images with good geometric convergence (e.g., see ALOS PRISM [11], ASTER [12], [13], IKONOS in-track stereo [14], and SPOT-5 HRS [1]), block adjustment with low overlap from weakly convergence geometry satellite images has seldom been discussed.

The main objective of this investigation is to propose a solution to solve the problem of weakly convergence geometry for satellite image blocks. Toutin [15] used elevation-added TPs in their method for block adjustment. The elevation of the TP is fixed to avoid the vertical error caused by weak convergence geometry. Since the planimetric coordinate of the TP is still unknown in the solution, the height of the TP is not easy to determine automatically. It is assumed that a DEM is available to provide a solution. We include an existing DEM in block adjustment. The elevation of the TP is fixed to avoid the vertical error caused by weak convergence geometry. Since the planimetric coordinate of the TP is still unknown in the solution, the height of the TP is not easy to determine automatically. It is assumed that a DEM is available to provide a solution. We include an existing DEM in block adjustment. Hence, the height of the TP must be iteratively interpolated from the DEM in the block adjustment process. Since the final goal is to produce orthoimages for landuse/landcover monitoring rather than 3-D surface reconstruction, the assumption of the availability of DEM is justified. In this investigation, we propose a revised block adjustment procedure including DEMs as elevation controls. Least squares collocation is integrated in the solution to compensate for systematic errors.

Three types of the block adjustment methods, namely, bundle adjustment, direct georeferencing, and RFM, are proposed in this investigation.

In the modified bundle adjustment method, there are three groups of observation equations including image coordinates with the collinearity condition, orientation parameters, and ground coordinates. Next, an elevation-controlled mechanism is proposed, which uses a DEM. The mechanism operates in such a way that the ground coordinates are iterated until simultaneously satisfying the collinearity condition, the ground surface, and the weighted orientation parameters. Finally, least squares collocation is included to adjust for local systematic errors.

In direct georeferencing, the observation vectors for the GCPs and TPs are formulated first. Preliminary fitting of the orbital parameters is employed when calculating all discrepancies for GCPs and the disparities for TPs. The discrepancy/parallax vectors are then employed for least squares collocation.

For implementation of elevation control in an RFM, a typical block adjustment is developed first. Since the RPCs are derived from precise GPS, INS, and star tracker data, they can be treated as constants. The block adjustment process necessitates the use of affine transformation and the observation equations of 3-D ground coordinates. In the adjustment process, the DEM is used as an elevation control. The ground coordinates are iterated until simultaneously satisfying the RFM, ground surface, and the weighted ground coordinates. Again, a least squares collocation is included.
numerical instability or projection error caused by a long track. In addition, the high correlation between orbital parameters and attitudes can be better depicted and separated during weighting.

The collinearity condition equations state that the exposure station, any object points, and its image point all lie along a straight line. The equations are modified, as in (1), to fit the imaging geometry of the satellite images. The exterior orientation parameters, including orbital and attitude, are characterized by second-order polynomials as functions of sampling time $t$ relative to the first scan line [17], i.e.,

$$x_i = \frac{-m_{11t}(X_i - X^c_t) + m_{12t}(Y_i - Y^c_t) + m_{13t}(Z_i - Z^c_t)}{m_{31t}(X_i - X^c_t) + m_{32t}(Y_i - Y^c_t) + m_{33t}(Z_i - Z^c_t)}$$

$$y_i = \frac{-m_{21t}(X_i - X^c_t) + m_{22t}(Y_i - Y^c_t) + m_{23t}(Z_i - Z^c_t)}{m_{31t}(X_i - X^c_t) + m_{32t}(Y_i - Y^c_t) + m_{33t}(Z_i - Z^c_t)}$$

where

- $x_i, y_i$ are photocoordinates at point $i$;
- $X_i, Y_i, Z_i$ are object coordinates at point $i$;
- $S_y$ scale affinity of CCD size;
- $f$ focal length;
- $X^c_t, Y^c_t, Z^c_t$ are exterior orbital parameters at time $t$;
- $m_{11t}, \ldots, m_{33t}$ are rotation matrix from attitude parameters at time $t$.

To distinguish the correlation between exterior orientation parameters, we include the pseudoequation and use a priori information for weighting. The pseudoequations [2] include the exterior orientation parameters and ground coordinates. Finally, the observation equation, pseudoequation for the exterior orientation parameter, and pseudoequation for the ground coordinates are combined. A least squares adjustment technique is applied to solve the unknown parameters. An in-depth description of the bundle adjustment can be found in [2].

The ray tracing technique is modified from [2] to determine the ground position of a TP. The ray tracing of the proposed bundle adjustment assumes that the orientation parameters, the DEM, and the coordinates of point are available. Since the orientation parameters are to be determined with the integration of the ray tracing, an iteration process is needed. This iterative procedure is used to determine the intersection point between the ray and the ground surface. The following are the three major processes in ray tracing: 1) calculation of the planimeter coordinates $(X, Y)$ for an initial elevation $Z$; 2) interpolation of the new elevation $Z'$ from the DEM according to planimeter coordinates $(X, Y)$; and 3) using interpolated elevation $Z'$ as the approximation value for the next iteration of the block adjustment. The iteration proceeds until the elevation variation is small enough.

After the ray tracing, the locations resulting from different orbits for the same TPs are not coincident. We take the average position of two ground points as the initial position of this TP. The weak geometry of the intersection gives rise to elevation errors that can be overcome by using DEM recursively during the least squares adjustment. Referring to Fig. 2, we see that the elevation $Z$ without prime denotes the elevation after bundle adjustment, and the $Z$ with prime denotes the elevation after interpolation in DEM. The subscripts of $Z$ indicate the number of iterations. The computation procedure starts from the initial value of $Z_1$ to $Z'_1$, moving to $Z_2$ and $Z'_2$, and so forth until convergence. This way, we can control elevation error within a reasonable range where convergence is expected.

### B. Direct Georeferencing

The direct georeferencing model comprises two major parts. In the first part, preliminary orbit fitting using the GCPs is carried out. In the second part, the orbit is refined by least squares collocation with TPs. A DEM is used as an elevation control in the block adjustment procedure. Fig. 3 illustrates the workflow of block adjustment with elevation control.

The satellite on-board data include orbital parameters and attitude data. We use the data to establish the state vectors of satellite position and the line of sight [18]. The state vectors are illustrated in Fig. 4. The collinearity condition equation for the state vectors is shown in (2). Once the exterior orientation parameters are modeled, the corresponding ground coordinates for an image pixel can be calculated. The GCPs are used to adjust the orbital parameters. Equation (3) is the collinearity equation with preliminary orbit fitting. To compensate the error for orbital parameters, a low-degree polynomial is applied in this state. We have

$$\vec{G} - \vec{P} = S\vec{U}$$  \hspace{1cm} (2)

$$\vec{G} - (\vec{P} + \Delta \vec{P}) = S\vec{U}$$  \hspace{1cm} (3)

where

- $\vec{G}$ ground point vector;
- $\vec{P}$ satellite position vector;
- $\vec{U}$ satellite line-of-sight vector;
- $S$ scale factor;
- $\Delta \vec{P}$ orbital polynomial function.

Geometric consistency is maintained between images by utilizing residual vectors on the TPs to reduce the image discrepancy. Thus, we need to compute the residual vectors for TPs.
First, we use the orbital parameters and the image coordinates of a TP to calculate the line of sight. Given a DEM, the ray tracing technique is then applied to determine the ground position of a TP. The following are the three major processes in ray tracing: 1) calculation of the planimeter coordinates \((X, Y)\) for an initial elevation \(Z\); 2) interpolation of the new elevation \(Z'\) from the DEM according to planimeter coordinates \((X, Y)\); and 3) using interpolated elevation \(Z'\) as the approximation value for the next iteration until the distance between intersection point and DEM is convergent. The procedure is repeated for its counterpart in the other image. As can be seen in Fig. 5, there are two ground corresponding points for each pair of TPs. This indicates discrepancy between the images. The center of two ground points is used as a constraint. The residual vector for each TP is the vector from one ground position to the middle of the two points.

Block adjustment is carried out by employing the discrepancy vectors of these TPs in a least squares collocation. The results after least squares collocation are shown in Fig. 6. In the
process, we assume that the $x$, $y$, and $z$ axes are independent. Three 1-D functions are applied to adjust the orbit. The model of least squares collocation [19] is shown in the following equation:

$$S_k = \sigma_k \cdot \Sigma_k^{-1} \cdot l_k$$  \hspace{1cm} (4)

where

- $k$ : $x$, $y$, and $z$ axes;
- $S_k$ : correct value of the interpolated point;
- $\sigma_k$ : row covariance matrix for the interpolated point with respect to the TPs;
- $\Sigma_k$ : covariance matrix for the TPs;
- $l_k$ : residual vectors for the TPs.

To determine the value of the covariance matrix, we select a Gaussian function with some empirical values for the covariance function [19], as shown in the following equation:

$$C = \begin{cases} (1 - r_n) \mu_k \exp\left(-(\frac{d}{d_{\max}})^2\right), & \text{if } d \neq 0 \\ \mu_k, & \text{if } d = 0 \end{cases}$$  \hspace{1cm} (5)

where

- $C$ : element of covariance matrix;
- $d$ : distance between intersection point and TP;
- $d_{\max}$ : maximum distance of intersection point;
- $\mu_k$ : variance of TPs’ residual;
- $r_n$ : filtering ratio, in which we use 0.2 in the experiment.

This empirical value 2.146 is selected so that the covariance limit is $1\% \times (1 - r_n)\mu_k$ when $d = d_{\max}$.

### C. RFM

The proposed method is also composed of two parts, namely, RFM-based block adjustment, and elevation control with DEM.

The RFM uses the ratio of two cubic polynomials to the RPCs. The RPCs are determined by fitting the physical camera model to describe the relationship between object space and image space [20]. To maintain numerical precision, the object and image space coordinates will be normalized to $(−1, +1)$.

General forms of RFM can be written as

$$x = \sum_{i=0}^{n_1} \sum_{j=0}^{n_2} \sum_{k=0}^{n_3} c_{ijk} X^i Y^j Z^K$$
$$y = \sum_{i=0}^{n_1} \sum_{j=0}^{n_2} \sum_{k=0}^{n_3} d_{ijk} X^i Y^j Z^K$$
$$z = \sum_{i=0}^{n_1} \sum_{j=0}^{n_2} \sum_{k=0}^{n_3} e_{ijk} X^i Y^j Z^K$$
$$f = \sum_{i=0}^{n_1} \sum_{j=0}^{n_2} \sum_{k=0}^{n_3} f_{ijk} X^i Y^j Z^K$$  \hspace{1cm} (6)

where

- $x, y$ : image coordinates;
- $X, Y, Z$ : object coordinates;
- $c_{ijk}, d_{ijk}, e_{ijk}, f_{ijk}$ : polynomial coefficients.

The coefficients of the RFM are called RPCs. Typically, since the RPCs are selected to the third degree, 80 coefficients are essentially included. There are two approaches for determining the RPCs. The first one is the GCP-derived RPC approach in which the coefficients are derived from numerous GCPs. However, this approach requires too many GCPs and, therefore, is considered unrealistic. The second option is the sensor-oriented RPC approach, which utilizes the on-board orientation of the satellite, including the orbital parameters and attitude data to generate enough transformation anchor points. This method can achieve high precision provided the on-board orbital parameters and attitude data are accurate. As most high-resolution satellites are equipped with instruments such as GPS, INS, and star trackers, they are capable of providing satisfactory orientation measurements. Accordingly, sensor-oriented RPCs are employed in this investigation. Fig. 7 illustrates the workflow of RFM block adjustment with elevation control.

To compensate for the systematic bias of the RPCs, we use an affine transformation to correct the error in the image space [21], [22]. The affine model is used to compensate the original image space and RFM’s image space. As the RPCs are calculated from the on-board data, the quality of RPCs is referred to the quality of on-board data. Due to the small FOV (e.g., SPOT is $4^\circ$) and the high precision of RPCs, the displacements in a small area may be assumed to be linear. Hence, an affine transformation might be applied to compensate the bias between original image space and RFM’s image space. The coefficients for the affine transformation can be calculated from the GCPs. The equation for the affine transformation is

$$S_{GCP} = a_0 + a_1 \cdot S_{RFM} + a_2 \cdot L_{RFM}$$
$$L_{GCP} = b_0 + b_1 \cdot S_{RFM} + b_2 \cdot L_{RFM}$$  \hspace{1cm} (7)

where

- $S_{GCP}, L_{GCP}$ : image coordinates of the GCP;
- $S_{RFM}, L_{RFM}$ : image coordinates determined by RFM;
- $a_0, b_0$ : affine coefficients.

The least squares form of the RFM equations can be represented in matrix form, as in (8). In turn, the matrix form can be
The matrix form of (10) is represented in a compact matrix notation as

\[
V_{ij} + B'_{ij} \Delta_j + B''_{ij} \Delta''_j = \varepsilon_{ij}
\]  

where

- \(V_{ij}\) residual matrix for the RFM equations;
- \(B'_{ij}, B''_{ij}\) observation matrices for the RFM equations;
- \(\Delta_j, \Delta''_j\) matrix of unknown parameters;
- \(\varepsilon_{ij}\) approximation matrix;
- \(i\) number of points;
- \(j\) number of images.

Block adjustment can enhance the geometric consistency between the images to improve their accuracy for orientation determination. The observation equations for the RFM and object coordinates are included in the block adjustment process. Since the affine coefficients are not highly correlated, we only include the pseudoequation observations for the object coordinates, without doing this for the affine coefficients. The pseudoequation for ground coordinates is formulated in (10). The matrix form of (10) is represented in a compact matrix notation as

\[
\begin{bmatrix}
V'_{Xi} \\
V'_{Yi} \\
V'_{Zi}
\end{bmatrix} - \begin{bmatrix}
\delta X_i \\
\delta Y_i \\
\delta Z_i
\end{bmatrix} = \begin{bmatrix}
dX_i \\
dY_i \\
dZ_i
\end{bmatrix}
\]  

\[V''_{ij} - \Delta''_j = C''_{ij}
\]  

\[
W' = \begin{bmatrix} W' & 0 \\ 0 & W'' \end{bmatrix}
\]

where

- \(V', V''\) residuals matrix for the pseudoequation;
- \(\Delta', \Delta''\) matrix of unknown parameters;
- \(C''_{ij}\) approximation matrix of measurement.

The combined observation equations can be written as (12). The weight matrix is shown in (13). The weight of the image coordinate is determined by the priori standard error of the image coordinate. We use 0.5 pixels as the standard error in this investigation. The weight of the ground coordinate is related to the standard error of the control point and TP. The standard error of the control point is referred to the measurement accuracy. The standard error of TP is ten times the control point. We have

\[
\begin{bmatrix} V' \\ V'' \end{bmatrix} + \begin{bmatrix} B' & B'' \end{bmatrix} \begin{bmatrix} \Delta' \\ \Delta'' \end{bmatrix} = \begin{bmatrix} \varepsilon \\ C'' \end{bmatrix}
\]  

\[
W = \begin{bmatrix} W' & 0 \\ 0 & W'' \end{bmatrix}
\]

Due to the weak convergence, a DEM is also included in the block adjustment as an elevation control. The idea of this elevation control is same as the modified bundle adjustment procedure. First, using the new planimetric coordinates \((X', Y')\) for each block adjustment iteration, we interpolate a new elevation \(Z'\) from the DEM and apply the elevation \(Z'\) for the next iteration of the block adjustment. Through iteration and interpolation, we attain an accurate result and overcome the problem of elevation error.

**D. Accuracy Analysis**

Four types of points, namely GCPs, control TPs, independent check points (ICPs) and independent check TPs (ICTPs), are included in the validation. After block adjustment, we use ICPs and ICTPs for accuracy analysis. The ICPs are used to check the
absolute accuracy as the ground coordinates of points are available. We use the orientation parameters, image coordinates, and height of ICP to calculate the ground coordinates. The difference between calculated and actual ground coordinates are used to evaluate the absolute accuracy of image.

The role of ICTPs is to evaluate the relative accuracy between images. An ICTP delivers image coordinates in two images. Each image coordinate may calculate a ground coordinate using the ray tracing technique with a DEM. The distance between these two ground coordinates can evaluate the relative accuracy between images. We also calculate the root mean square error (RMSE) of ICPs and ICTP as the indices for accuracy analysis.

The resulting single adjustment is also provided to compare the performance of single and block adjustments. The DEM is not needed for single adjustment. The single adjustment performs the geometric correction strip by strip. The block adjustment performs the adjustment for strips simultaneously. Since the single adjustment uses GCPs only, there is no need for a DEM. In the modified bundle adjustment, the single adjustment uses collinearity equations with GCP to calculate the orientation parameters without using TP and pseudoequations. In the direct georeferencing, the single adjustment uses state-vector collinearity equations with GCP to calculate the unknown parameters without using TP or least squares collocation. In the RFM, the single adjustment uses affine transformation with GCP to calculate the unknown parameters without using TP and pseudoequations.

### III. Experimental Result

The test data include three SPOT 5 supermode panchromatic image strips. In each experiment, we test two cases, with different numbers of scenes. Case I contains one standard scene per strip, while case II contains two. The test areas are in the center part of Taiwan stretching from the west coast to the east coast, as shown in Fig. 8(a) and (b). The strips have about 10%–15% overlap, as shown in the figure. GCPs and ICPs are acquired from 1 : 5000 scaled topographic maps. GCP accuracy is estimated to be better than 3 m. The TPs and ICTPs are acquired by manual measurements. The terrain of the test site has about 3800 m relief, as shown in Fig. 8(c) and (d). The vertical accuracy of DEM is estimated at about 3 m for nonhilly area. The vertical accuracy in the hilly area could be larger than the estimated value. Information related to the test images is given in Table I. Before the geometric correction, we use all the ground points to evaluate the accuracy of on-board data. Table II shows the mean error and RMSE of both cases. The accuracy is better than 50 m, which reflects the specifications of SPOT-5 [23].

The validation experiments are carried out in three parts. First, the geometrical consistency between strips is evaluated; second, the absolute accuracy is examined; and finally, mosaicked images generated from the derived orientation parameters are checked. In this section, the “Modified Bundle Adjustment,” “Direct Georeferencing,” and “RFM” are indicated by MBA, DG, and RFM, respectively. Since the SPOT image provides only on-board data, we generate 80 sensor-oriented RPCs for each of the SPOT images using the method in [24].

#### Table I

<table>
<thead>
<tr>
<th>Description</th>
<th>Strip 1</th>
<th>Strip 2</th>
<th>Strip 3</th>
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<tr>
<td>Date</td>
<td>2003/6/21</td>
<td>2003/5/31</td>
<td>2003/7/1</td>
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<tr>
<td>Incidence Angle (Deg)</td>
<td>5.21°</td>
<td>5.65°</td>
<td>-14.76°</td>
</tr>
<tr>
<td>GSD (m)</td>
<td>2.52</td>
<td>2.52</td>
<td>2.67</td>
</tr>
<tr>
<td>Overlapping Area</td>
<td>10%</td>
<td>15%</td>
<td></td>
</tr>
<tr>
<td>Image Size</td>
<td>24000*24000 (Supermode)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Number of GCPs</td>
<td>9</td>
<td>9</td>
<td>9</td>
</tr>
<tr>
<td>Number of ICPs</td>
<td>25</td>
<td>11</td>
<td>11</td>
</tr>
<tr>
<td>Number of TPs</td>
<td>19</td>
<td>13</td>
<td></td>
</tr>
<tr>
<td>Number of ICTPs</td>
<td>18</td>
<td>13</td>
<td></td>
</tr>
<tr>
<td>Image Size</td>
<td>24000*48000 (Supermode)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Number of GCPs</td>
<td>20</td>
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<td>22</td>
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<td>Number of ICPs</td>
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<tr>
<td>Number of TPs</td>
<td>32</td>
<td>26</td>
<td></td>
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<tr>
<td>Number of ICTPs</td>
<td>31</td>
<td>26</td>
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<tr>
<td>DEM</td>
<td>40m Topographic Data Base of Taiwan</td>
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<tr>
<td>Elevation Range</td>
<td>0m-3800m</td>
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#### Table II

<table>
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<tr>
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<th>Strip1</th>
<th>Strip2</th>
<th>Strip3</th>
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<td>Case I</td>
<td>E</td>
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<tr>
<td>Mean</td>
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<td>29.09</td>
<td>-1.93</td>
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<tr>
<td>RMSE</td>
<td>16.38</td>
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<tr>
<td>Case II</td>
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<tr>
<td>Mean</td>
<td>15.95</td>
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<tr>
<td>RMSE</td>
<td>16.34</td>
<td>29.37</td>
<td>5.89</td>
</tr>
</tbody>
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#### A. Geometrical Consistency Between Strips

Case I: We choose a pair of TPs that appear in two images. A pair of TPs delivers two image coordinates in two images. Each image coordinate may calculate a ground position using
Table III: Comparison of Geometrical Consistency (Case I)

<table>
<thead>
<tr>
<th>Units: meters</th>
<th>Types</th>
<th>RMSE</th>
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<tbody>
<tr>
<td></td>
<td>Strips 1 &amp; 2</td>
<td>No. TP=19</td>
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<td></td>
<td>No. ICTP=18</td>
<td></td>
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<tr>
<td>MBA</td>
<td>Block TP</td>
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<tr>
<td></td>
<td>ICTP</td>
<td>1.22</td>
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<td></td>
<td>Single ICTP</td>
<td>11.56</td>
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<tr>
<td></td>
<td>Improvement</td>
<td>ICTP</td>
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<tr>
<td>DG</td>
<td>Block TP</td>
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<td></td>
<td>ICTP</td>
<td>2.55</td>
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<td>Single ICTP</td>
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<tr>
<td></td>
<td>Improvement</td>
<td>ICTP</td>
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<tr>
<td>RFM</td>
<td>Block TP</td>
<td>2.69</td>
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<td>2.68</td>
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<td>Improvement</td>
<td>ICTP</td>
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</tbody>
</table>

The ray tracing technique with DEM and orientation parameters. Hence, a pair of TPs may obtain two ground positions from two images. The ground positions of TP are checked using ICTPs. Distance between these two ground positions is used to evaluate the discrepancy. Table III illustrates the accuracy of the performance of using ICTPs for single image adjustment and block adjustment. The error vector for strips 1 and 2 after block adjustment is shown in Fig. 9(a)–(c); the error vector for strips 2 and 3 is shown in Fig. 9(d)–(f). Triangles indicate TPs, while circles represent the ICTPs. It can be seen that the error vectors for the three proposed methods are very similar.

The RMSE for the ICTP for strips 1 and 2 prior to the block adjustment is larger than 6.5 m. After block adjustment, it is better than 2.7 m. For strips 2 and 3, RMSE of ICTP is improved from 22 and 28 m to 6 and 5 m in the east and north directions, respectively. Significant improvement of geometrical consistency is demonstrated when TPs are employed in the block adjustment. The range of improvement is from 4 to 24 m. The difference obtained with the three methods is less than 1 m (i.e., 0.4 pixels). This is the case for all strips after block adjustment except when the RFM is in the east direction (for strips 2 and 3) because of the tradeoff phenomenon in the block adjustment. The phenomenon reveals the balance of GCPs and TPs that makes the relative accuracy improved with marginal degradations of absolute accuracy.

Case II: In case II, there are two standard scenes in a strip. Hence, the total number is six standard scenes. The geometrical consistency between strips is checked by measuring the TPs. The numbers of TPs in the overlapping area are 32 for strips 1 and 2 and 26 for strips 2 and 3. The numbers of check TPs are 31 for strips 1 and 2 and 26 for strips 2 and 3. The adjustment results with and without block adjustment are shown in Table IV. The results of geometrical consistency without block adjustment using MBA and DG are very similar. Before block adjustment, the geometrical consistency of single strip adjustment is around 10 m for strips 1 and 2. The geometrical consistency between strips 2 and 3 is only around 18 m due to the hilly terrain. After block adjustment, the geometrical consistency of strips 1 and 2 has improved to 2.5 m and...
the geometrical consistency between strips 2 and 3 is better than 4.5 m when MBA and DG are applied. The significant improvement of geometrical consistency shows the importance of using block adjustment. Note that the range of improvement is from 3 to 14 m.

The behavior of RFM is different from the other two methods. Although the results for geometrical consistency in single strip adjustment are better than the other methods, the RFM block adjustment results are less accurate.

### B. Absolute Accuracy

**Case I:** The absolute accuracy is evaluated using ICPs. This test includes a comparison of the three proposed block adjustment methods. The results of single image adjustment are also provided for comparison. Table V shows the single image adjustment results obtained using each of the three methods. The numbers of GCPs and ICPs are also indicated. The result for strip 3 is around 7 m due to the 15° viewing angle and the high terrain relief. The absolute accuracy of strip 1 is better than that of strip 2 because the terrain relief is less extreme. The difference between these three methods is less than 1.8 m (i.e., 0.7 pixels) for all strips. Error vectors indicate no obvious difference and the error direction is similar. The points near the overlapping area are affected by the constraint on the TPs.

### TABLE VI

<table>
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<th>Units: meters</th>
<th>Strips 1</th>
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<td>DG</td>
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Fig. 10. Error vectors for strip 1 (case I). (a) DG. (b) MBA. (c) RFM.
Case II: The absolute accuracy results obtained with the three single strip adjustment methods for case II are shown as Table VII. The same GCPs and ICPs are applied with each method for comparison. The numbers of GCPs and ICPs are also indicated in the table. The performance of these three methods for the three strips is very similar. The difference of ICP is less than 1 m between the three models, which means that for single image adjustment, they may provide similar results. The absolute accuracy of these three strips ranges from 3.0 to 6.0 m.

The results of block adjustment with DEM control are provided in Table VIII. In addition to the GCP, we also include the TPs used for image stitching. Comparing Tables VII and VIII, we see that the results of block adjustment are similar to those of single strip adjustment for strips 1, 2, and 3. The performance of block adjustment is less than for single strip adjustment. This phenomenon is similar to case I. This could be due to the influence of the coarse DEM for the steep area.

C. Image Mosaicking

The results obtained with the three methods are consistent. We select one case, i.e., case II, and the modified bundle...
adjustment method and examine the geometrical consistency of the image mosaicking. The locations of the mosaicked images with respect to the block are shown in Fig. 13. For ease of comparison, two enlargements are shown in Fig. 14. In Fig. 14(a), we find obvious discontinuity. This condition is significantly improved in Fig. 14(b)–(d), where it is also show that the block adjustment may improve the geometrical consistency.

D. Summary of the Experimental Results

The experimental results are summarized as follows.
1) The geometric performances of the three proposed methods are similar.
2) The proposed methods offer significant improvement in the geometric consistency between overlapping images with respect to the single image adjustment by about a factor of 5.
3) The RMSE of ICPs increases slightly when block adjustment is employed.
4) It is expected that in extremely rough mountain areas, the DEM will be less accurate than the GCPs and ICPs. This could explain the improvement in geometric with the deterioration of the RMSE of the check points. Nevertheless, the payoff reveals the effectiveness of the block adjustment process.

IV. CONCLUSION

In this paper, we have compared three approaches to block adjustment for satellite images with weak convergence geometry using DEM as the elevation control. The first method is a revised version of traditional bundle adjustment. The second is based on the direct georeferencing approach. The third is an RFM with sensor-oriented RPCs. The experimental results indicate that the proposed DEM elevation control method can significantly improve the geometric accuracy as well as reduce discrepancies. The range of improvement is from 3 to 24 m in different cases. The results from the three block adjustment methods are consistent. Tests indicate that the proposed method should be feasible for real applications.

The resolution of the DEM in this study is 40 m, which is not favorable for mountain areas. If the quality of the DEM is improved, higher accuracy may be expected. In future work, more data sets will be validated when DEMs with better quality are available. In this investigation, we use the multiple images taken from a single satellite. Since many other satellites are available, block adjustment with different sensors becomes an important work. The future research will focus on the integration of heterogeneous sensor models.

REFERENCES


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